Cognitive abilities, sociocultural background and academic achievement

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The influence of students’ sociocultural background on academic achievement is a well established fact. Research also points out that sociocultural background is related to students’ cognitive abilities and these have an effect on their academic achievement. However, the mediator role of cognitive abilities on the relationship between sociocultural background and academic achievement is less well known. A structural equation model that represents these relationships was tested in a sample (N= 728) of Portuguese junior high school students. Multigroup analysis of the model showed the importance of the cognitive ability mediation effect between sociocultural background and academic achievement in the 7th and 9th grades, but not in the 8th grade. This difference may be the result of the academic transition experienced in the 7th and 9th grades in the Portuguese educational system, which requires parents’ higher involvement in school.

Various studies conducted since the 1960s emphasize the contribution of socio-familial variables to students’ learning and academic achievement (AA). Coleman and colleagues in 1966 (Coleman, 1988) became famous in this regard, as they not only succeeded in demonstrating the relevance of the family sociocultural background (SCB), but also the relevance of an intervention to overcome deficits at this level.

There is a significant connection between the students’ AA and their families’ SCB. Higher levels of parents’ education — in particular of mothers— generate greater expectations, attendance and help concerning the children’s school work (Davis-Kean, 2005). This kind of attendance may compensate for the students’ learning difficulties, and may contribute to overcome some of the failures pointed out in the educational system itself. Research conducted in various countries and among various ethnic groups confirms the relevance of the family factors in explaining the students’ learning process (Dumka, Gonzales, Bonds, & Millsap, 2009; Engin-Demir, 2009; Flouri & Buchanan, 2004; López, Calvo, & Caro, 2008). There is the conviction that parents’ educational styles and attendance of the school activities are positively related with students’ self-esteem and self-concept, becoming the students intrinsically motivated for learning and AA (García & Sánchez, 2005; Gonzalez-Pienda et al., 2002; López et al., 2008).

Along with parents’ SCB, other factors are equally important in explaining the students’ AA. Namely, the students’ cognitive abilities (CA) continue to be researched and are assumed to be a determinant factor in learning and AA. The cognitive functions used in the definition and measurement of intelligence are, after all, required in learning situations. These intellectual capacities are related to SCB (Colom & Flores-Mendoza, 2007; Deary, Strand, Smith, & Fernandes, 2007; Floyd, Evans, & McGrew, 2003; Taub, Floyd, Keith, & McGrew, 2008).

The influence of students’ SCB on CA and on AA, and of CA on AA, are acquired facts. However, the mediation role of CA on the relationship between SCB and AA is, as far as we know, not yet studied. We intend to assess the impact of students’ CA on the predictive relationship between their SCB and their AA in the three sequential years of the Portuguese third cycle of studies; 7th, 8th and 9th grades. We examine if the direct effect of SCB on AA (higher SCB, higher AA) is reinforced by the indirect effect of SCB on AA, represented by the effect of students’ SCB on their CA (higher SCB, higher CA) and the effect of students’ CA on their AA (higher CA, higher AA). In Figure 1, we present the conceptual
The latent construct SCB was operationalized through the educational and professional level of students’ parents. Five levels to the former (level 1 = 4th grade; level 2 = 5th and 6th grades; level 3 = 7th, 8th and 9th grades; level 4 = 10th, 11th and 12th grades; and, level 5 > 12th grade), and three levels to the latter: level 1= low (unskilled workers in commerce, services, agriculture, fishing, construction, industry and transports); level 2= medium (salesmen, skilled workers in agriculture and fishing, technicians and administrative professionals); level 3= high (upper management and specialists in intellectual and scientific professions).

The latent construct AA was operationalized through the students’ marks (from 1 to 5) in the disciplines of Portuguese (Port.), English (Eng.), mathematics (Math.) and nature sciences (NC).

Data analysis

The SPSS for Windows (version 17.0) was used for descriptive data analysis. Participants with missing values and outliers were excluded. The model was tested using LISREL 8.53 (Jöreskog & Sörbom, 2002).

In a multigroup cross-sectional study with LISREL, measurement invariance of discrete data, like the ordered-categorical data generated for both SCB and AA, implies a specific kind of parameterization (Jöreskog, 2005; Millsap & Yun-Tein, 2004). PRELIS 2 (Jöreskog & Sörbom, 1996) uses the indicators’ underlying latent continuous response cut by m - 1 threshold parameters (m = number of response options) to produce the means and the polychoric covariance matrix of that latent variables, along with their asymptotic covariance matrix. The first two thresholds are fixed to zero and one respectively (Millsap & Yun-Tein, 2004). Estimates were computed for each group under fixed thresholds to the pooled thresholds estimates in the combined group. The means and the covariance matrices of this multigroup analysis were used as input to LISREL.

Model estimation was done using the SIMPLIS command language (Jöreskog & Sörbom, 1993) with the Satorra-Bentler scaled correction of maximum likelihood (MLsb; Satorra & Bentler, 1994), which adjusts standard errors and model fit statistics to nonnormality. This robust technique performs very well over different sample sizes and degrees of nonnormality with continuous (Curran, West, & Finch, 1996) and discrete (DiStefano, 2002) variables.

The MLsbχ2, the comparative fit index (CFI) and the root mean square error of approximation (RMSEA) were used in this study to evaluate the goodness of fit (GOF) of the hypothesized model to empirical data. The χ2 is an absolute measure of the discrepancy between model and data: a level of probability lower than .05 for the χ2 indicates lack of fit (Jöreskog & Sörbom, 1993). The CFI compares the model with its’ null counterpart, the independence model, indicating the amount of data covariation that is reproduced by the model: it must be .90 to accept the model (by convention) and close or above .95 to show a good fit (Hu & Bentler, 1998). The RMSEA is a measure of the discrepancy per degree of freedom between model and data: a value below .06 indicate a good fit (Hu & Bentler, 1998).

Following Jöreskog and Sörbom’s (1993) two-step approach of modeling, the confirmatory factor analysis (CFA) of the measurement model with the three latent constructs freely correlated (oblique factor model) was done before the assessment of the structural relationships of the PMLV for SCB influence on AA. To assure construct validity, it is important that latent constructs present acceptable convergent
validity (CV), discriminant validity (DV) and reliability (Anderson & Gerbing, 1988). To assign the latent constructs’ units of measurement, the relationship for one of its indicators was fixed to one.

Measurement equivalence across groups typically begins with the test of the configural invariance of the model. In this model all parameters are freely estimated across groups. As a baseline model, it serves a process of testing more stringent equality conditions across groups. Meredith (1993) pointed out three types of measurement invariance: weak, strong and strict. In the first type, the factor loadings are equal over groups (all the other parameters are freely estimated). In the second, the factor loadings plus the fitted means or intercepts (values of each indicator corresponding to the zero value of the factor) are equal over groups. In the third, besides factor loadings and intercepts, also the residuals (indicators’ specific factor plus random error) are equal over groups. Strong invariance is necessary for comparisons of latent construct means, because it assures that constructs have the same scale over groups (i.e., the same origin and unit of measurement). Likewise, strong invariance is necessary to test multigroup equality of regression models with latent variables (Jöreskog & Sörbom, 1993).

When full invariance is not achieved, partial invariance can be reached by allowing a subset of indicators to vary freely across groups, while constraining at least one to equality in addition to those that are equal due to their being fixed to unity for identification purposes (Byrne et al., 1989). Nevertheless, data-driven modifications of an initial model should be substantively justified to avoid capitalization on chance (MacCallum, Roznowski, & Necowitz, 1992).

The assessment of model fit in testing model equivalence is usually founded in GOF statistics, in addition to chi-square tests. However, the excessive sensitivity of the $\chi^2$ test statistic to sample size and model complexity led to alternative approaches. The use of the CFI’s change ($\Delta$CFI) between a full model (model with parameters unconstrained in all groups) and a restricted model (model with specific parameters constrained to equality across groups) is recommended to overcome that problem (Cheung & Rensvold, 2002). A $\Delta$CFI higher than .01 indicates noninvariance of the restricted model.

The $\text{ML}_{\text{ce}}$ estimates for the completely standardized solution (with both factors and indicators standardized) to common metric of the measurement invariant model allowed the examination of latent constructs’ CV, DV, and composite reliability (CR) (Fornell & Larcker, 1981). The CV was assessed through the indicators’ average variance extracted (AVE), which should be at least .50. The DV was assessed by comparing the shared variance (square disattenuated correlation) between any two constructs and the AVE of each: the values of the former should be lower than those of the latter. Construct’s reliability is deemed acceptable for group comparisons when it reaches .80 (Nunnally & Bernstein, 1994).

The unstandardized solution of the tested model (Figure 1) was used to examine its structural relationships, with one-tail t-Student tests because of the well established nature of model’s relationships (higher x, higher y). The expression $\Delta$CE $= (\gamma_{10} - \gamma_{11})$/root square $[(SE_{\gamma_{10}}^2 + SE_{\gamma_{11}}^2)/2]$ was used to assess the CA’s mediation in the predictive relationship between SCB and AA. In this expression: $\gamma_{10} =$ unstandardized total effect (equal to unstandardized direct effect + unstandardized indirect effect) of SCB on AA; $\gamma_{11} =$ unstandardized direct effect of SCB on AA, with $SE_{\gamma_{10}}$ and $SE_{\gamma_{11}}$ as respective standard errors. A $\Delta$ test statistic higher than 1.96 indicates that the compared effects differ at the $p<.05$ significance level: CA has a reinforcement effect.

Results

Measurement equivalence

The results of the CFA showed that form invariance of the measurement model across groups was not tenable because of the lack of reliability of MR subtest in the 9th grade group (B=.19, 

<table>
<thead>
<tr>
<th>Indicator</th>
<th>7th grade (n=269)</th>
<th>8th grade (n=210)</th>
<th>9th grade (n=249)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\beta$</td>
<td>$R^2$</td>
<td>Intercept</td>
</tr>
<tr>
<td>MEL</td>
<td>.93</td>
<td>.90</td>
<td>.57</td>
</tr>
<tr>
<td>MPL</td>
<td>1.05</td>
<td>.90</td>
<td>-1.62</td>
</tr>
<tr>
<td>FEL</td>
<td>.79</td>
<td>.72</td>
<td>.08</td>
</tr>
<tr>
<td>FPL</td>
<td>.63</td>
<td>.90</td>
<td>-.91</td>
</tr>
<tr>
<td>AR</td>
<td>.40</td>
<td>.49</td>
<td>4.82</td>
</tr>
<tr>
<td>NR</td>
<td>.43</td>
<td>.26</td>
<td>7.53</td>
</tr>
<tr>
<td>VR</td>
<td>.67</td>
<td>.37</td>
<td>11.00</td>
</tr>
<tr>
<td>SR</td>
<td>.57</td>
<td>.38</td>
<td>8.14</td>
</tr>
<tr>
<td>Port.</td>
<td>.90</td>
<td>.87</td>
<td>.45</td>
</tr>
<tr>
<td>Eng.</td>
<td>.90</td>
<td>.64</td>
<td>.58</td>
</tr>
<tr>
<td>Math.</td>
<td>.60</td>
<td>.90</td>
<td>1.10</td>
</tr>
<tr>
<td>NC</td>
<td>.91</td>
<td>.65</td>
<td>.67</td>
</tr>
</tbody>
</table>

Note: MEL= mother educational level; MPL= mother professional level; FEL= father educational level; FPL= father professional level; AR= abstract reasoning; NR= numerical reasoning; VR= verbal reasoning; SR= spatial reasoning; Port= mark in Portuguese; Eng= mark in English; Math= mark in mathematics; NC= mark in nature sciences. $\beta$= standardized factor loading (with $p<.001$); $R^2$ (communality) = 1 - $r$ (standardized residual)
Partial weak invariance model (the covariances of latent constructs were constrained to data over groups (MLsb \( \chi^2 = 175.60, df = 173, p = ns; \text{CFI} = .895; \text{RMSEA} = .008 \)). To make this model invariant (MLsb \( \chi^2 = 161.73, df = 164, p = ns; \text{CFI} = .901; \text{RMSEA} = .000 \)), it was necessary to freely estimate the intercepts of FEL and Math. in the 8th grade group, plus those of FEL and NC in the 9th grade group (see Table 1).

Nevertheless, the number of indicators in the 9th grade group with loadings and intercepts that needed to be unconstrained was too high to be acceptable (MPL, FPL and FEL), violating the standard of factor level invariance (Byrne et al., 1989). Hence, strict measurement invariance and factor level invariance were not assessed for completeness.

Finally, through MLsb estimates of the completely standardized solution to common metric for the partial weak invariant model, excellent CV and CR were verified in all groups for SCB (AVE between .84 and .83; CR = .95) and AA (AVE between .75 and .62; CR between .92 and .86). Nevertheless, both CV and CR were weak in all groups for CA (AVE between .42 and .34; CR between .74 and .66). Regarding the latent constructs’ DV, all their shared variances were lower than the AVE of each one, with the exception of those obtained in the 7th grade group for both SCB and CA (.49) and CA and AA (.86), and the one obtained in the 9th grade group for CA and AA (.52).

Overall, the results of the CFA for the partial weak invariant model provided some evidence for construct validity (with major problems for CA in the 7th grade group), and this model was used to test the structural relationships of the PMLV for SCB influence on AA, with the direct effects, the variance of SCB and the structural residuals of CA and AA freely estimated across groups.

### Structural relationships

The specified PMLV for SCB influence on AA was well fitted to data. The GOF statistics presented in the caption of Figure 2 are, as expected, identical to those of the partial weak measurement invariant model (the covariances of latent constructs were respescted as direct effects). For simplicity purposes, only the structural relationships are presented in the figure.

We can see through the MLsb estimates for the model’s unstandardized solution that all the direct effects are statistically significant in all groups, with two nuances in the effect of SCB on AA (higher SCB, higher AA), which is both less significant than the other effects in all groups and less significant in the 8th grade group than in the other groups. Also the magnitude of the effect of SCB on CA (higher SCB, higher CA) is lower in the 8th grade group than in the other groups, and the magnitude of the effect of CA on AA (higher CA, higher AA) is lower in the 9th grade group than in the other groups. Comparing the effects that constitute the indirect effect of SCB on AA, the one of SCB on CA is higher than the one of CA on AA in all groups.

Overall, the indirect and the total effects of SCB on AA were higher in both the 7th and 9th grade groups than in the 8th grade group, and the coefficients of determination (R²) of CA and AA present the same pattern.

Finally, the MLsb estimates for the unstandardized solution also pointed out that the statistical significance of the difference between the direct effect and the total effect of SCB on AA was tenable for both the 7th (\( \Delta \chi^2 = 247.33, p = ns \)) and 9th (\( \Delta \chi^2 = 162.21, p = ns \)) grade groups, but not in the 8th grade group (\( \Delta \chi^2 = 181, p = ns \)).

<table>
<thead>
<tr>
<th>Grade</th>
<th>Model Estimate</th>
<th></th>
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</thead>
<tbody>
<tr>
<td>7th</td>
<td>SCB</td>
<td>CA</td>
<td>AA</td>
<td></td>
</tr>
<tr>
<td>R²</td>
<td>0.350</td>
<td></td>
<td>0.483</td>
<td></td>
</tr>
<tr>
<td>Indirect effect SCB-CH-AA</td>
<td>0.113 (.025)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total effect SCB-AA</td>
<td>0.199 (.024)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>8th</td>
<td>SCB</td>
<td>CA</td>
<td>AA</td>
<td></td>
</tr>
<tr>
<td>R²</td>
<td>0.152</td>
<td></td>
<td>0.284</td>
<td></td>
</tr>
<tr>
<td>Indirect effect SCB-CH-AA</td>
<td>0.069 (.018)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total effect SCB-AA</td>
<td>0.142 (.030)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>9th</td>
<td>SCB</td>
<td>CA</td>
<td>AA</td>
<td></td>
</tr>
<tr>
<td>R²</td>
<td>0.240</td>
<td></td>
<td>0.284</td>
<td></td>
</tr>
<tr>
<td>Indirect effect SCB-CH-AA</td>
<td>0.075 (.032)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total effect SCB-AA</td>
<td>0.161 (.017)</td>
<td></td>
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</tbody>
</table>

**Figure 2.** Path Model with Latent Variables for Sociocultural Background Influence on Academic Achievement: Unstandardized maximum likelihood estimates for structural relationships. Goodness of fit statistics: MLsb \( \chi^2 = 162.21, df = 164, p = ns; \text{CFI} = .901; \text{RMSEA} = .008 \). Standard errors in parenthesis. R² (coefficient of determination)= amount of the latent criteria’s variance accounted by latent predictor(s). See Figure 1 for other abbreviations.

**Discussion**

Following a two-step approach of modeling (Anderson & Gerbing, 1988; Jöreskog & Sörbom, 1993), we tested, in 7th, 8th, and 9th grade students, a PMLV for SCB influence on AA to assess
the impact of CA on the predictive relationship between SCB and AA.

At measurement level, the test of form invariance led to the exclusion of MR. The model without MR was only weak invariant (Meredith, 1993) over groups, and in a partial way (Byrne et al., 1989). Once data-driven modifications of a model can be due to chance characteristics of the data set (MacCallum et al., 1992), their substantive justifications are: (1) the MR subtest includes items involving academic knowledge (e.g., from physic principles) or practical competencies (daily problem-solving strategies), and these different type of contents explain it’s reliability problems to represent CA; (2) the MPL and FPL’s group differences were due to random differences in sample characteristics; (3) the AR’s difference between the 7th and the 8th grade groups can be explained through normative age-graded developmental gains (Almeida & Lemos, 2007); (4) the NR’s difference between the 8th and the 9th grade groups can be explained as later developmental consequences of the previous changes in AR; and, (5) the Engl. group differences can be explained based on changes in curricular demands (higher with the grades passing by).

Because the necessary condition of strong invariance (Meredith, 1993) to test multigroup equivalence of regression models with latent variables (Jöreskog & Sörbom, 1993) was not verified, the structural relationships of the PMLV for SCB influence on AA were assessed without equality constraints across groups.

The model was well fitted to data and, as expected considering the previously reviewed literature, all its structural relationships were statistically significant in all groups. Study’s results also showed that the pattern of model’s structural relationships was analogous in the 7th and 9th grade groups, but different to the one of the 8th grade group. The same can be said about the impact of students’ CA on the predictive relationship between their SCB and their AA: CA had a reinforcement role on the effect of SCB on AA in the 7th and 9th grade groups, but not in the the 8th grade group. Overall, there is a similar pattern in the beginning and in the end, but not in the middle, of this cycle of studies. This difference can be related with a higher parent’s involvement in school transition years.

The PMLV for SCB influence on AA was analysed in terms of its «predictive accuracy within the same domain of prediction as that from which the observed data were sampled» (interpolative predictive accuracy, Forster, 2002, p. S126). The convenience sampling procedure of this research imposes limitations in model extrapolation and, moreover, in model generalization: the study of various non-probabilistic samples or, better, of a representative sample, is desirable. The study of the model equivalence across time would also illuminate if the changes found in this study for the 8th grade students were not artefacts created by its cross-sectional nature. Furthermore, knowing that parent involvement, with the mediation of academic self-concept (ASC), has a positive effect in AA (González-Pienda et al., 2002) the model might be improved with another indirect path including the ASC.

Some practical implications can be presented considering this study. The impact of SCB in students’ AA was confirmed namely in the transition grades when it’s expected a bigger involvement of parents in their adolescents’ academic activities. So, particular attention must be given to students belonging to lowest social status, for example an enrichment curriculum or a parents’ education program promoting their investment on children’s academic activities. This study shows that the socio-familiar impact on academic achievement increases when we introduce in data analysis the students’ CA, which is particularly evident when students are involved in transition schools years. Cognitive training programs should be provided to students who cumulatively come from lower socio-familiar stratus and present low cognitive abilities. These students show patterns of self-concept, motivation and CA not favorable to a successful academic achievement. These academic fragilities can assume particular relevance in transition school grades, when some new disciplines or some vocational options are presented.

References


